

Sets and Venn Diagrams

Thursday, Aug 29th

How can we represent mathematical information more simply on a diagram or in a set?

What classifies a finite set?

* A set is a collection of numbers or objects

$$A = \{0, 1, 2, 3, 4, 5, 6, 7, 8, 9\}$$

- Written within brackets
- Separated by commas
- Use capital letters to represent sets

How do I represent the info in a Venn diagram?

* The numbers or objects in a set are called ELEMENTS or MEMBERS of the set

- \in = element of
- \notin = not an element of
- \mathbb{Q} = rational #'s $\frac{p}{q}$ and $q \neq 0$
- \mathbb{R} = set of all real #'s

* The set $\{ \}$ or \emptyset is called the EMPTY SET and contains no elements

- $\mathbb{N} = \{0, 1, 2, 3, 4, 5, 6, 7, \dots\}$ Natural counting numbers
- $\mathbb{Z} = \{0, \pm 1, \pm 2, \pm 3, \pm 4, \dots\}$ Integers
- $\mathbb{Z}^+ = \{1, 2, 3, 4, 5, 6, 7, \dots\}$ Positive Integers
- $\mathbb{Z}^- = \{-1, -2, -3, -4, -5, \dots\}$ Negative Integers

Counting Elements of Sets

* The number of elements in Set A is written $n(A)$
ex) $A = \{2, 3, 5, 8, 13, 21\} = 6$ elements so $n(A) = 6$

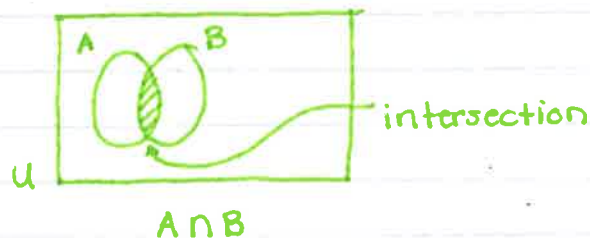
* A set which has a finite # of elements is called a finite set

ex) $A = \{2, 3, 5, 8, 13, 21\}$ is a finite set
 \emptyset is also a finite set, since $n(\emptyset) = 0$

* Infinite sets are sets which have infinitely many elements

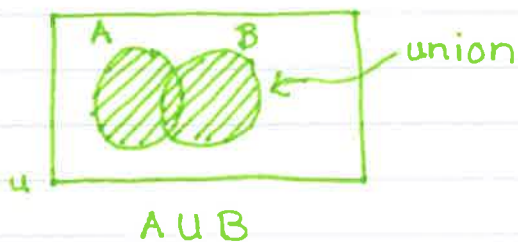
Intersection

* $A \cap B$ consists of all elements common to both A and B. It is the shaded region where the circles representing A and B overlap.



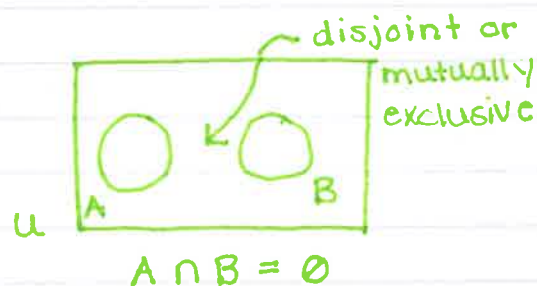
Union

* $A \cup B$ consists of all elements in A or B or both. It includes both circles.



Disjoint or Mutually Exclusive Sets.

* Disjoint sets do not have common elements. They are represented by non overlapping circles.



$$* n(A \cup B) = n(A) + n(B) - n(A \cap B)$$

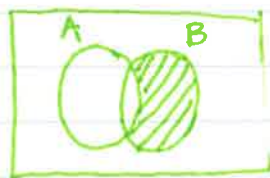
$$* n(A \cap B) = n(A) + n(B) - n(A \cup B)$$

Subsets

P is a subset of Q if every element of P is also an element of Q

$$\text{ex) } P = \{1, 2, 3, 4\} \quad Q = \{1, 2, 3, 4\}$$
$$P \subseteq Q$$

Shading Diagrams



$$A' \cap B$$

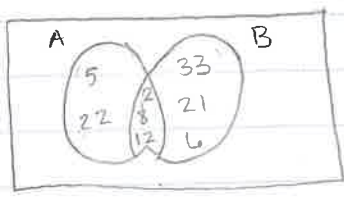


$$(A \cap B)'$$



$$A = \{2, 5, 8, 12, 22\}$$

$$B = \{2, 6, 8, 12, 21, 33\}$$

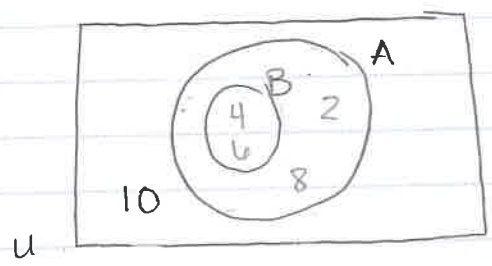


$n(A \cap B) = 3$
number of intersection #

$$U = \{2, 4, 6, 8, 10\}$$

$$A = \{2, 4, 6, 8\}$$

$$B = \{4, 6\}$$



- BCA
- ACU
- BCU