

$$\text{Theta} = \theta$$

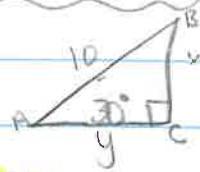
## Trigonometric Ratios

How can you use the three trigonometric ratios to solve for an unknown angle in any triangle?

Why can't I solve this?

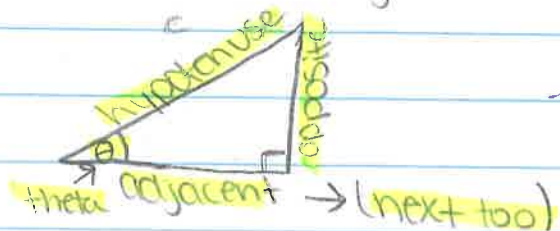
There are two variables.

Solve for x and y



Can you use Pythagorean theorem to solve for c?

no but you can use trig.

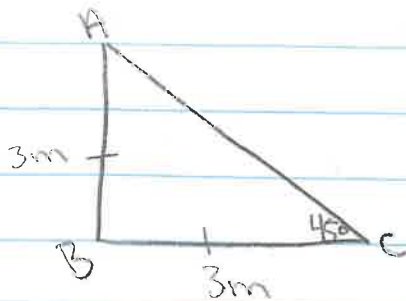


## Sine, cosine, tan

$$1. \sin \theta = \frac{\text{opp}}{\text{hyp}}$$

$$2. \cos \theta = \frac{\text{adj}}{\text{hyp}}$$

$$3. \tan \theta = \frac{\text{opp}}{\text{adj}}$$



$$\text{Theta } \theta = 45^\circ$$

$$\text{opp} : 3\text{m}$$

$$\text{adj} : 3\text{m}$$

$$\sin(\theta) = \frac{\text{opp}}{\text{hyp}}$$

$$\sin(45^\circ) = \frac{3}{c}$$

$$c = 4.24\text{m}$$

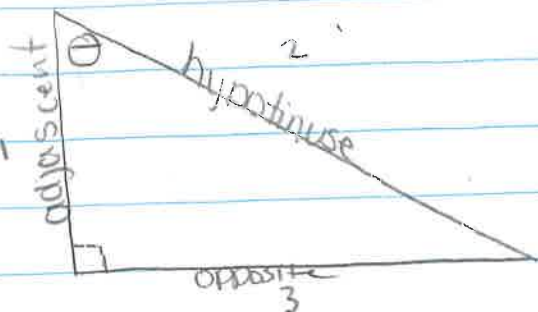
$$c \cdot .7071 = 3 \cdot c$$

$$c \cdot \frac{.7071}{.7071} = \frac{3 \cdot c}{.7071}$$

Theta

⊖

α alpha

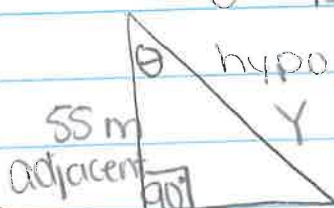
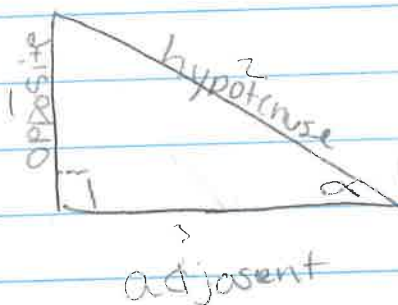


Theta = 40°

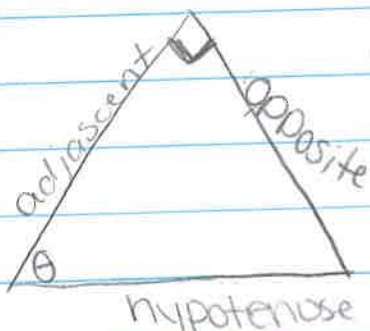
adjacent = 55

opposite = x

⊖ = 40°



Tan(⊖) 40°

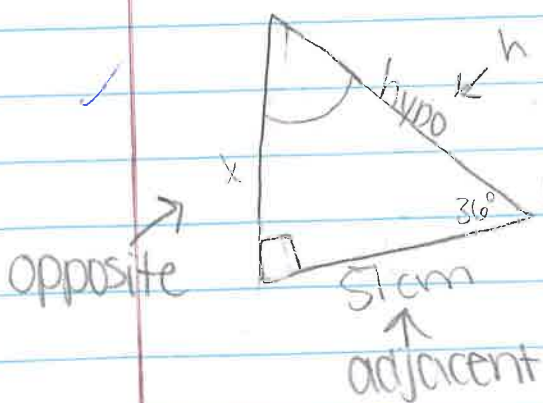


55 · Tan(⊖) 40° =  $\frac{x}{55}$

55 · Tan(40°) = x

416.15 = x

Soh caa Toa



⊖ theta = 36°

⊖ adjacent = 51 cm

⊖ opposite = x = 37.026 cm

h · Sin(⊖) 36° =  $\frac{37.026 \text{ cm}}{h}$

$\frac{h \cdot \text{Sin } 36^\circ}{.5877} = 37.026$

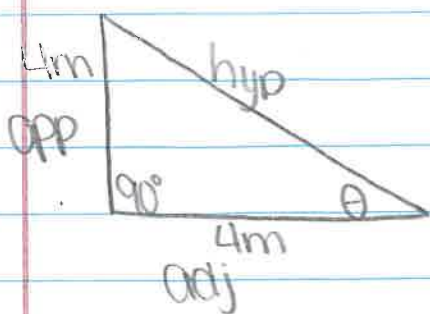
h = 63.00

51 · Tan(⊖) (36°) =  $\frac{x}{51}$

51 cm · Tan(36°) = x

37.026 = x





$$4^2 + 4^2 = C^2$$

$$16 + 16 = C^2$$

$$32 = C^2$$

$$5.65 = C$$

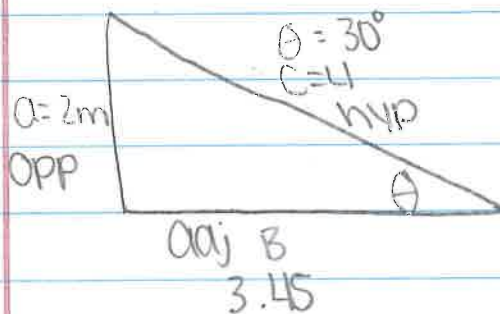
$$\sin(\theta) = \frac{\text{OPP}}{\text{hyp}}$$

$$\sin(\theta) = \frac{4m}{5.65}$$

$$\approx .7071$$

$$\cos(\theta) = \frac{4m}{5.65} \approx .7071$$

$$\tan(\theta) = \frac{4m}{4m} \approx 1$$



Opp = 2m  
hypotenuse?

$$C \cdot \sin(30^\circ) = \frac{2m}{C} \cdot C$$

$$C \cdot \sin(30^\circ) = 2m$$

$$C \cdot \frac{.5}{.5} = \frac{2m}{.5}$$

$$C = 2m = 4$$

$$2^2 + B^2 = 4^2$$

$$4 + b^2 = 16 \quad \tan(30) = \frac{2}{b}$$

$$B^2 = 12$$

$$B = 3.46$$

(SOH) (CAH) (TOA)

$$B \cdot .577 = \frac{2 \cdot b}{b}$$

Sine =  $\frac{\text{opposite side}}{\text{hypotenuse}}$

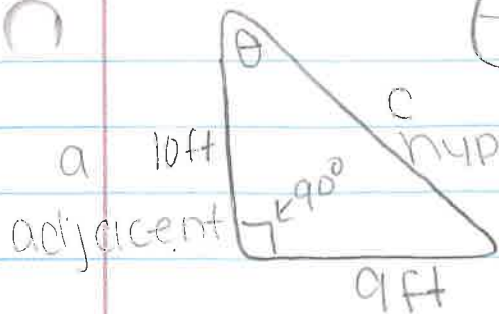
$$B \cdot .577 = \frac{2}{.577}$$

cosine =  $\frac{\text{adjacent side}}{\text{hypotenuse}}$

tangent =  $\frac{\text{opposite side}}{\text{adjacent side}}$

○

# (Trig Notes)



How can we solve for an unknown angle?

OPPOSITE

b

$$\tan(\theta) = \frac{9}{10}$$

$$\tan(\theta) = .9$$

Theta = ?

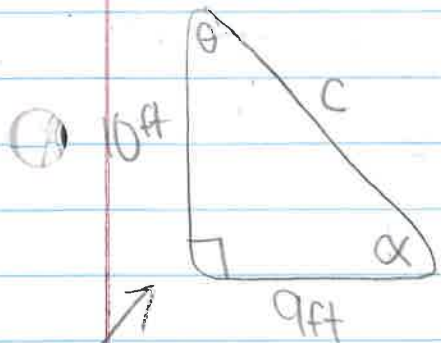
OPPOSITE = 9ft

$$\tan^{-1} \tan(\theta) = .9 \tan^{-1}$$

ADJACENT = 10ft

$$(\theta) = \tan^{-1} .9$$

$$(\theta) = 41.99$$



Pythagorean and theorem.

$$a^2 + b^2 = c^2$$

$$10^2 + 9^2 = c^2$$

$$100 + 81 = c^2$$

$$181 = c^2$$

$$\sqrt{181} = 13.45 \text{ft}$$

inverse function

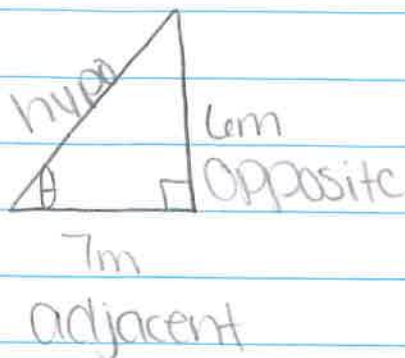
Sin<sup>-1</sup>

cos<sup>-1</sup>

Tan<sup>-1</sup>

Solve for  $(\theta)$

What do we know?



Theta?

$$\text{opposite } 6\text{m} = \text{Tan}$$

$$\text{adjacent } 7\text{m}$$

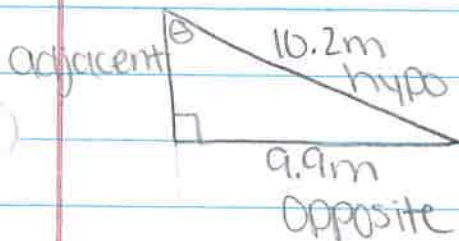
$$\text{Tan } (\theta) = \frac{6}{7}$$

$$\text{Tan } (\theta) = 0.86$$

$$\text{Tan}^{-1} \text{Tan } (\theta) = 0.86 \text{tan}^{-1}$$

$$(\theta) = \text{Tan}^{-1} 0.86$$

$$(\theta) = 40.7 \text{ m}$$



Theta?

hypo 10.2

Opposite 9.9

$$\text{Sin } (\theta) = \frac{9.9}{10.2}$$

$$\text{Sin}^{-1} \text{Sin } (\theta) =$$

$$(\theta) =$$

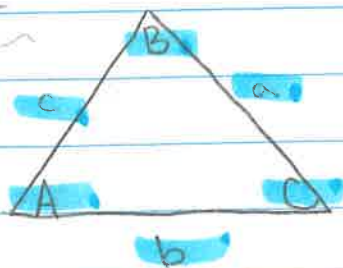
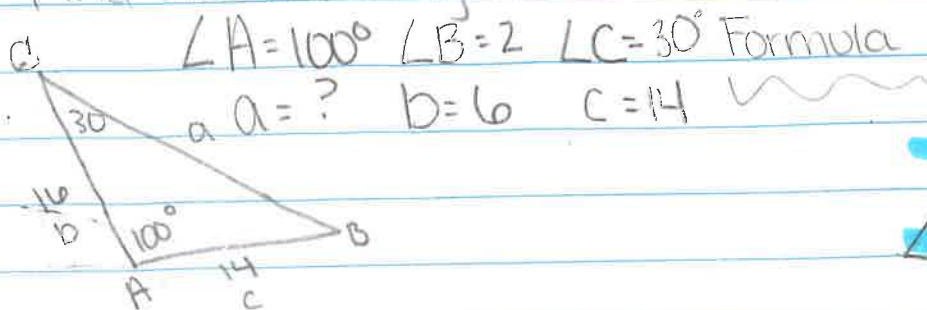
$$\text{Sin}^{-1} \rightarrow 9.90588235$$

$$\theta = 76.07$$



# Law of Sines

Find the missing measurement



$$\frac{\sin A}{a} = \frac{\sin B}{b} = \frac{\sin C}{c}$$

$$\frac{\sin(100^\circ)}{a} = \frac{\sin(30^\circ)}{14}$$

Big Letter = Angles  
Little Letter = Side length

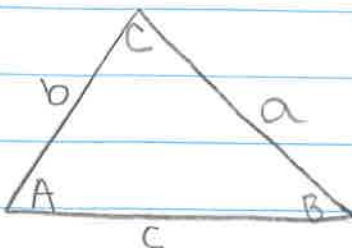
$$a \cdot \frac{.984807753}{a} = 0.035714286 \cdot a$$

$$\frac{.984807753}{.035714286} = .035714286 \cdot a$$

$$27.57 = a$$

Law of cosine

$$\text{Formula: } c^2 = a^2 + b^2 - 2ab \cos C$$



Use formula

$$\angle A = 410^\circ$$

$$a = ?$$

$$\angle B = ?$$

$$b = 200$$

$$\angle C = ?$$

$$c = ?$$

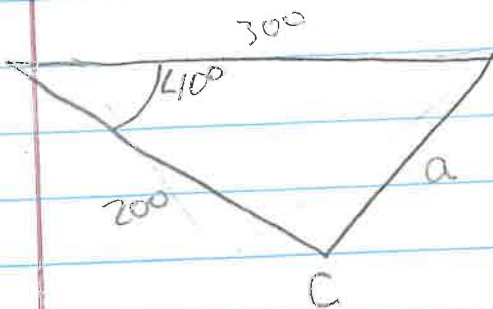
$$c^2 = a^2 + b^2 - 2ab \cos C$$

$$300^2 + 200^2 - 2(300)(200) \cos(410^\circ)$$

$$c^2 = 90,000 + 40,000 - 120,000 \cdot 7.660444131$$

$$c^2 = 90,000 + 40,000 - 91,925.33317$$

$$c^2 = 38074.66683$$



$$\angle A = A$$

$$a = 11 \text{ cm}$$

$$\angle B = B$$

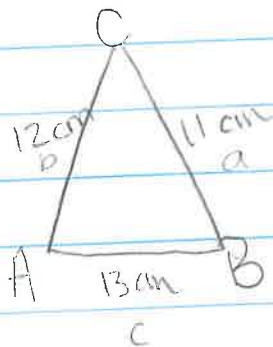
$$b = 12 \text{ cm}$$

$$\angle C = C$$

$$c = 13 \text{ cm}$$

Sin

\*cant  
Use  
Pythagorean  
+ theorem



$$c^2 = a^2 + b^2 - 2ab \cos C$$

$$13^2 = 11^2 + 12^2 - 2(11)(12) \cos C$$

$$169 = 121 + 144 - 2 \cdot 11 \cdot 12 \cos(C)$$

$$169 = 121 + 144 - 264 \cos(C)$$

$$169 = 265 - 264 \cos(C)$$

$$-265 \quad -265$$

$$-96 \quad -264 \cdot \cos(C)$$

$$-264 \quad -264$$

$$\cos^{-1} \frac{3636363636}{3636363636} = \cos(C) \cos^{-1}$$

$$108.66^\circ = C$$