

TOPIC: Trigonometric ratios

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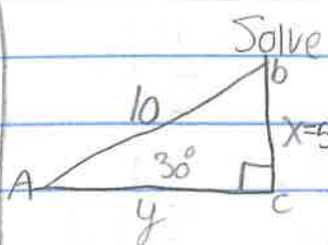
3-8-18

EQ: How can you use the three trigonometric ratios to solve for an unknown angle in any triangle?

Why can I not solve this?

I can't solve this because it has 2 variables.

Solve for $x + y$ $\theta = 30^\circ$ Hyp=10 opp= x adj= y



$\sin(30^\circ) = \frac{x}{10}$
 $10 \cdot .5 = \frac{x}{10}$
 $5 = x$

$\cos(30^\circ) = \frac{y}{10}$
 $10 \cdot .866 = \frac{y}{10}$
 $8.66 = y$

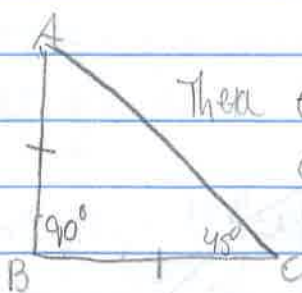
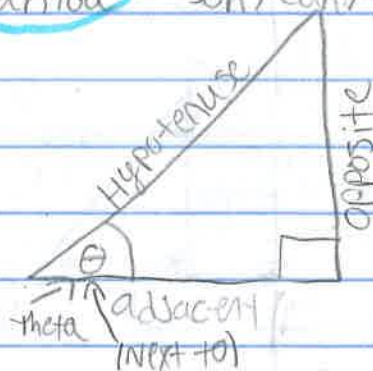
Acronym: Sohcahtoa Soh/cah/toa

3 equations

1. $\sin(\theta) = \frac{\text{opp}}{\text{hyp}}$

2. $\cos(\theta) = \frac{\text{adj}}{\text{hyp}}$

3. $\tan(\theta) = \frac{\text{opp}}{\text{adj}}$



Then $\theta = 45^\circ$

Opposite: 3m

adjacent: 3m

$\sin(\theta) = \frac{\text{opp}}{\text{hyp}}$

$\sin(45^\circ) = \frac{3}{c}$

$c \cdot .7071 = 3$

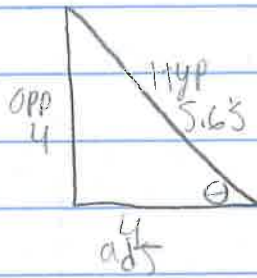
$c = \frac{3}{.7071} = 4.24$

$c = 4.24 \text{ m}$

$\alpha = \text{Alpha}$

✓ You can use the three trigonometric ratios to solve for an unknown angle by finding out where Hyp, adj, & opp are on a triangle. Also you need to know where Theta is.

Can you use
Pythagorean theorem
to solve for Hyp?
No but you
can use trig.



$$16 + 16 = c^2$$

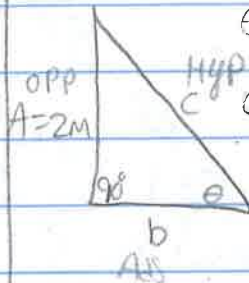
$$\sqrt{32} = \sqrt{c^2}$$

$$c = 5.65$$

$$\sin(\theta) = \frac{4}{5.65} = 0.7071 \quad \tan(\theta) = \frac{4}{4} = 1$$

$$\cos = \frac{4}{5.65}$$

$\theta = 30^\circ$ opp = 2m Hyp = 4m adj = ?



$$C \cdot \sin(30^\circ) = \frac{2m}{2}$$

$$C \cdot \sin(30^\circ) = 2m$$

$$C \cdot 0.5 = 2m$$

$$C = \frac{2m}{0.5} = 4$$

$$z + b^2 = 2^2$$

$$\frac{4}{b^2} = \frac{16}{16}$$

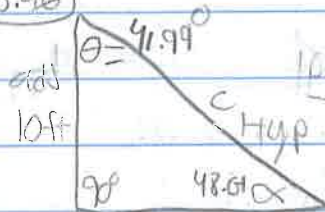
$$b = 3.46$$

$$b \cdot \tan(30^\circ) = \frac{z}{b}$$

$$b \cdot \tan(30^\circ) = z$$

$$b \cdot 0.577 = \frac{2}{0.577} \quad b = 3.46$$

How can we solve
for unknown angles



Inverse Function

$$\sin^{-1}, \cos^{-1}, \tan^{-1}$$

$$\tan(\theta) = \frac{9}{10}$$

$$\tan(\theta) = 0.9 \tan^{-1}$$

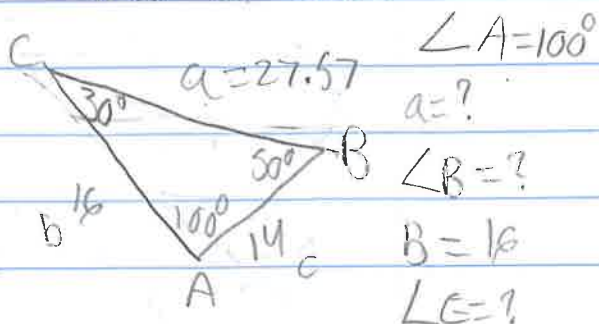
$$\theta = \tan^{-1}(0.9)$$

$$\theta = 41.99$$

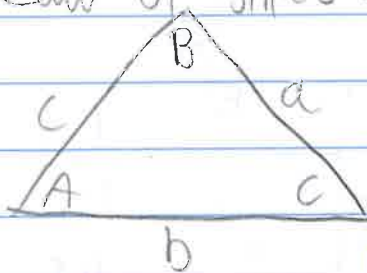
$$100 + 81 = c^2$$

$$\sqrt{181} = \sqrt{c^2} \quad c = 13.45$$

Law of Sines



Law of Sines $c = 14$



big letter - Angles
small letter - Side legs
Always across from

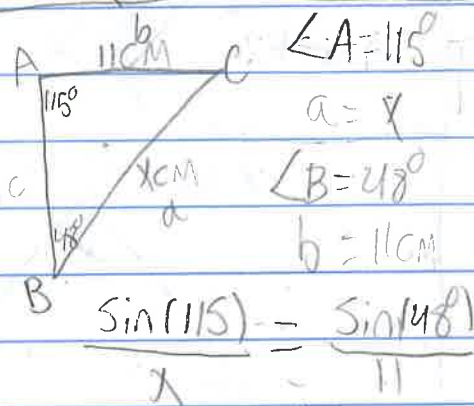
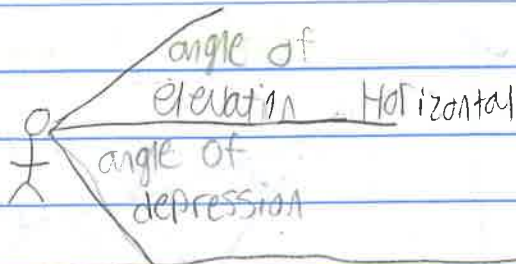
$$\frac{\sin A}{a} = \frac{\sin b}{b} = \frac{\sin c}{c} \text{ each other}$$

$$\frac{\sin(100^\circ)}{a} = \frac{\sin(30^\circ)}{14}$$

$$a \cdot .984807753 = .035714286 \cdot a$$

$$\frac{.984807753}{.035714286} = \frac{.035714286 \cdot a}{.035714286}$$

$$a = 27.57$$



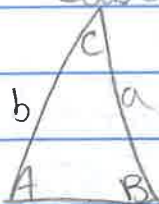
$$\frac{\sin(115)}{x} = \frac{\sin(48)}{11}$$

$$x = \frac{11 \cdot \sin(115)}{\sin(48)}$$

$\cdot 906307787$

Law of Cosines

$$c^2 = a^2 + b^2 - 2ab \cos C$$



$$13^2 = 11^2 + 12^2 - 2(11)(12) \cos(C)$$

$$169 = 121 + 144 - 264 \cos(C)$$

$$169 = 265 - 264 \cos(C)$$

$$-96 = -264 \cos(C)$$

$$\cos(C) = \frac{96}{264} = \frac{4}{11}$$

$$C = 68.68^\circ$$